

Probing Local ISM Turbulence using High-Fidelity Measurements of Cosmic Rays

M.A. Malkov

University of California San Diego

Collab.: Pat Diamond, Mingyun Cao (UCSD), Igor Moskalenko (Stanford U),

Research at UCSD supported by the US NSF Grant No. AST-2109103, at Stanford U. – by NASA,
80NSSC23K0169 and 80NSSC22K0718

Two Power Laws in the Milky Way (Jokipii, Armstrong, Rickett, Spangler...)

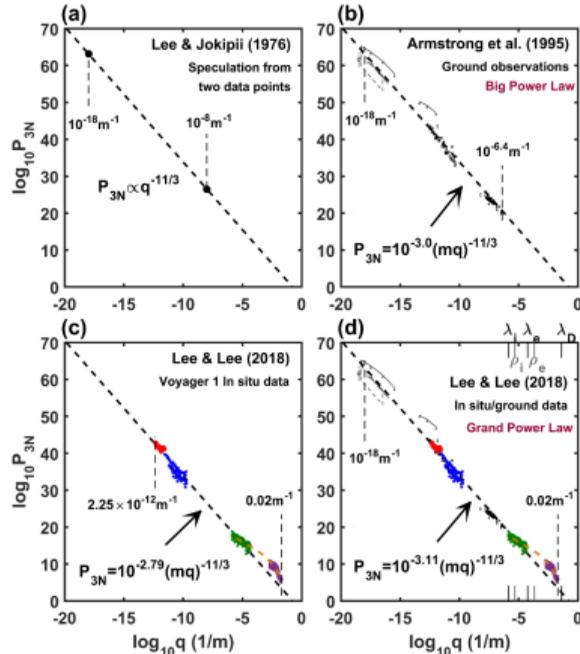
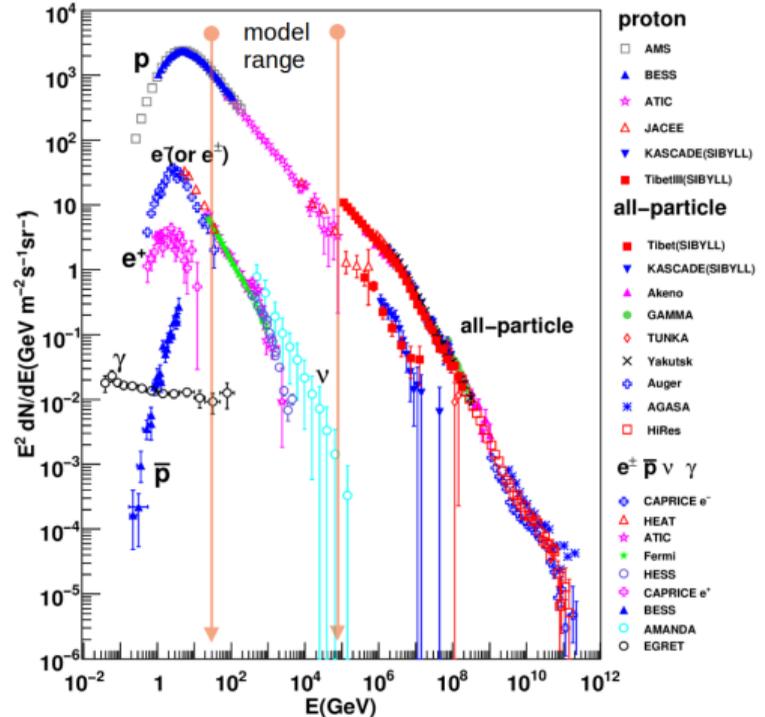


Figure 2 Interstellar turbulence spectra: (a) the Kolmogorov spectrum suggested by Lee & Jokipii (1976), (b) the Big Power Law by Armstrong et al. (1995), (c) the in situ spectrum obtained from Voyager 1 by Lee & Lee (2018), and (d) The Grand Power Law from combination of the ground remote observations (Armstrong et al., 1995; Chepurinov and Lazarian, 2010) and satellite in situ observations (Lee & Lee, 2018).

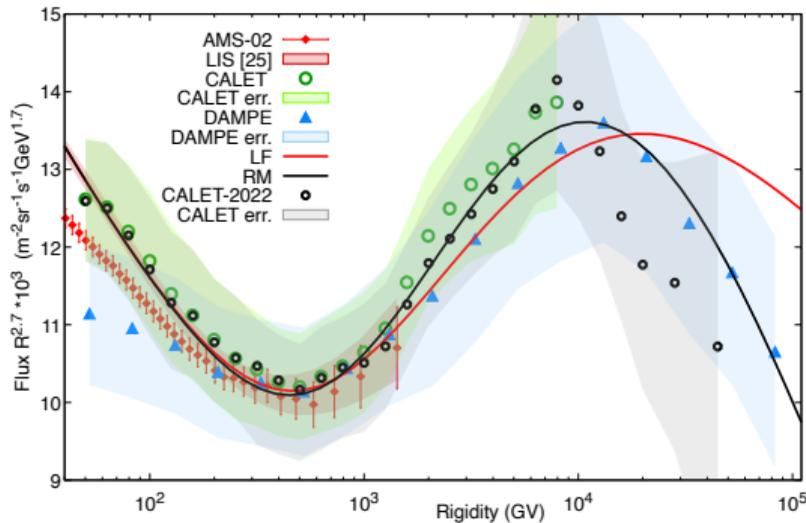
Lee, K-H. (2018)

Cosmic Ray Spectra (Hu arxiv:2009.00007)



- Key three instruments: AMS-02, CALET, DAMPE...
- **10-TeV CR Bump: what is it?**
 - SNRs, ISM propagation? small-scale anisotropy \equiv **means local source, closer than a few m.f.p.**
 - freshly-accelerated particles? secondaries are at least a million-year old
 - Superposition of sources or change in CR diffusivity? - breaks are too sharp
- CR source (reacceleration) is close to the Sun
 - **turbulence spectrum in the ISM between the source and observer can be extracted from the CR spectrum**
- need of new standards:
 - **number of free parameters vs number of descriptors**
 - ▶ pay due attention to the **fit accuracy**
 - ▶ **abandon log-log \rightarrow do log-linear plots!**

New data on the long-suspected CR bump/Calet Update



MM & I. Moskalenko, ApJ 2022, These authors
ICRC 2023

**-Incredibly sharp second break at ~ 10 TV
measured by CALET (!)**

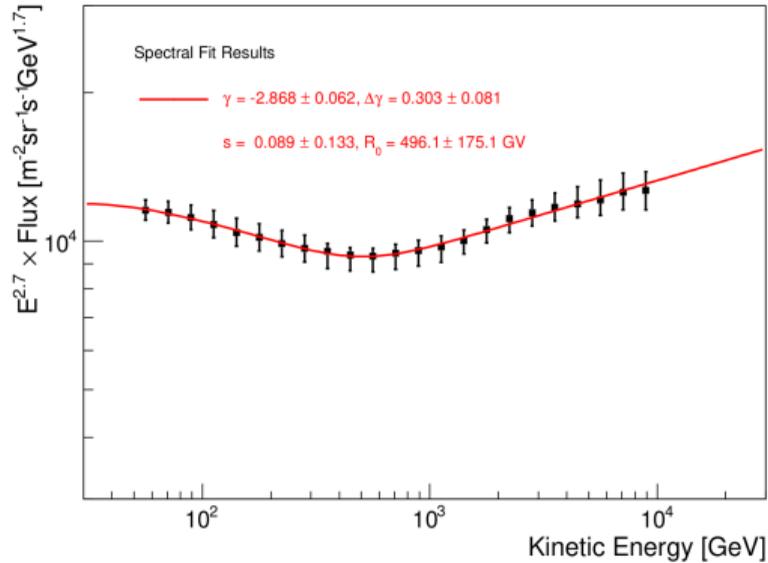
still consistent with DAMPE and the model
with particle losses from the magnetic flux tube

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- At first (CREAM, ATIC, **PAMELA** 2006-2011) detected a **dip** around $R_{br} \sim 200 - 300$ GV
- improved observations revealed a **second break** (softening), at $\gtrsim 10$ TV, initially by DAMPE, only
- now confirmed by CALET but much sharper!
- PAMELA's first break was even sharper than the current CALET's second break
- confirmed later by AMS-02, but shifted to $R_{br} \approx 450$ GV and **smoothed!**

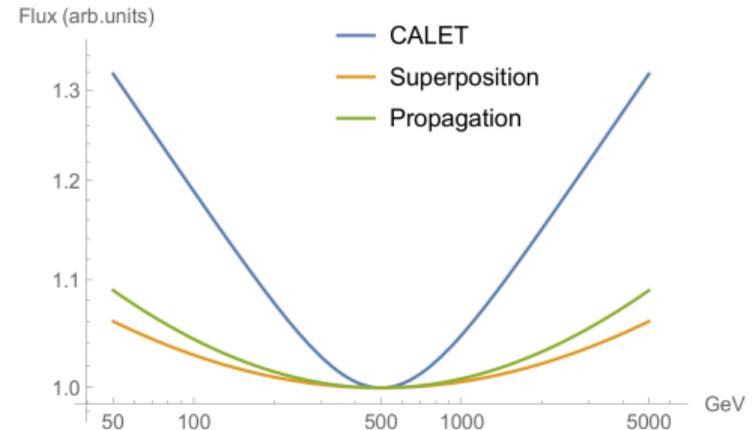
Parameters of the first break



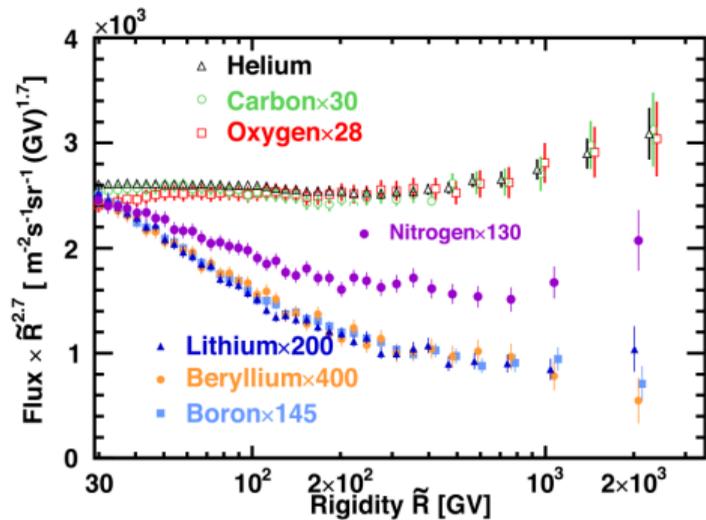
$$F \propto E^{-\gamma} \left[1 + (E/500)^{\Delta\gamma/s} \right]^s$$

$$\Delta\gamma = 0.3, \quad s = 0.1$$

- Attempts to fit Calet data to a superposition of two sources or by breaking the CR diffusion scaling with energy result in a very smooth transition between the two power-laws



Secondary Elements Test

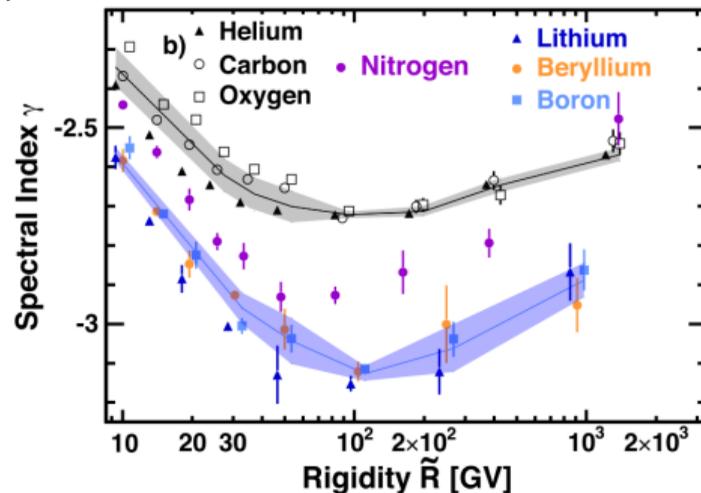


AMS-02, PhRep,

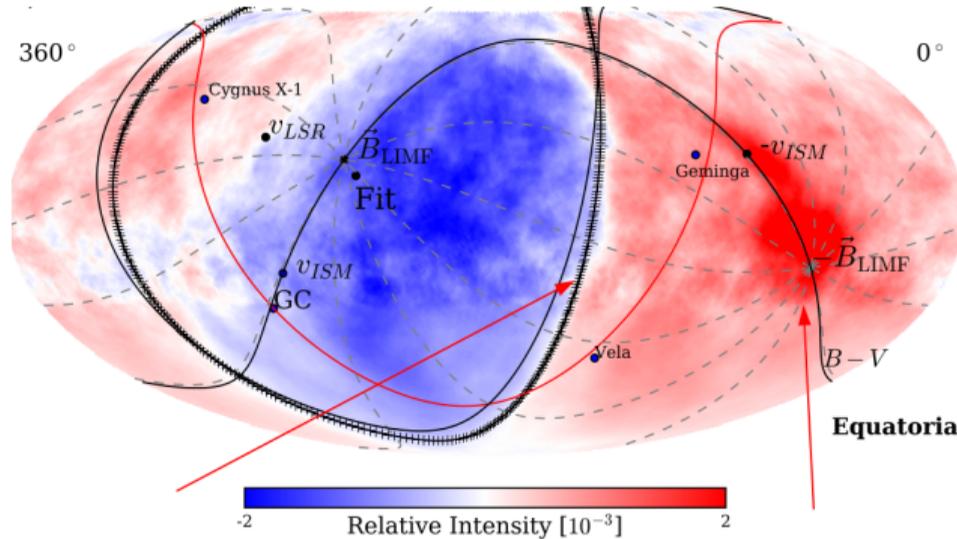
2021

- Were the flattening coming from a different source with harder spectrum, it wouldn't be the same for all the primaries and all the secondaries
 - fragmentation and production cross sections are different

- Spectral shapes of primaries are similar
- Spectral shapes of secondaries are also similar, but different from the primaries
- spectra of secondaries are steeper than primaries for all R



Small-Scale Anisotropy



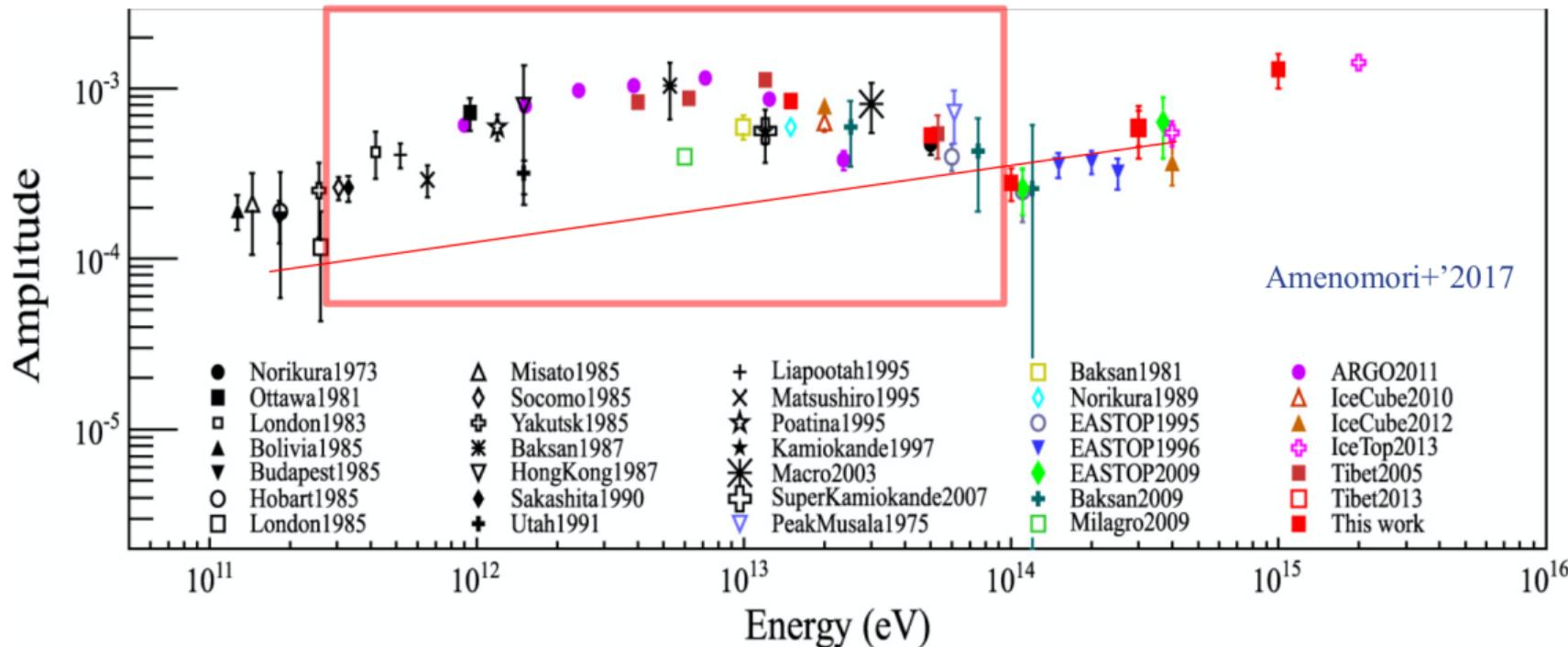
- **Observations** (Abeysekara+2019)

- two key signatures constraining the distance to their source:

- CR intensity jump across magnetic horizon
 $\mu = \cos \vartheta \approx 0$
- enhancement in the field direction
 $\mu \approx 1$

- Note, that a similar field-aligned CR proton beam in the 10 TV range has been observed by Milagro

Dipole Anisotropy in the Bump Area



$$\bullet \quad \mathbf{v} \cdot \nabla f \sim \frac{\partial}{\partial \mu} D \frac{\partial f}{\partial \mu} \rightarrow \quad \kappa \sim \frac{c^2}{D}$$

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$$\bullet \quad \frac{1}{f} \frac{\partial f}{\partial \mu} \sim \frac{\kappa}{c L_{\text{source}}} \sim \frac{3}{c} \cdot \frac{10^{26} - 10^{28}}{3 - 300 \text{ pc}} \sim 10^{-3}$$

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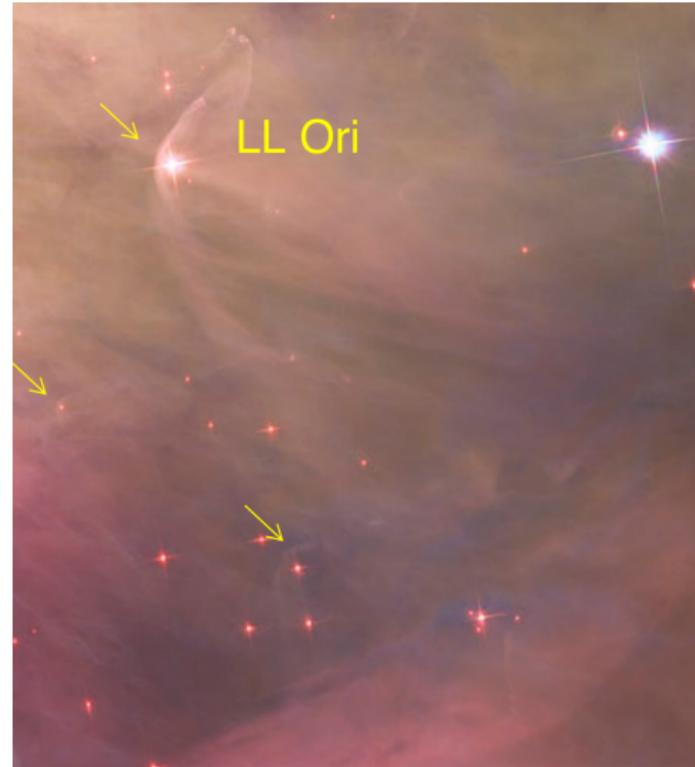
INITIAL Model Assumptions: Weak Shock in the Local Bubble

- distance to the shock within 3-10 pc
- $T \sim 10^6 K$, a 100 km/s shock $\rightarrow M = 1.4 - 1.7$
- rarefied plasma, $n \sim 0.01$, $\beta \sim 2$
- can be old SNR (radiative shell, e.g., Chevalier 1974)
- bow-shock of a rapid star, via outer Lindblad resonant scattering (Dehnen 1999)
- can be a termination shock of strong stellar wind. **Reacceleration**

Example:

Hubble image of Orion Nebula \rightarrow

- **As CR-reaccelerating shock and Heliosphere are moving through the ISM, only the CRs with sufficient rigidity can reach us**



Solution at a Shock for and Propagation Upstream of reaccelerated CRs

- start with the solution upstream of a bow-shock (Blandford&Ostriker, 1978)

$$f(x, R) = f_\infty \left\{ 1 + \frac{\gamma_s + 2}{q - \gamma_s} \exp \left[-u_1 \int_0^x \frac{dx'}{\kappa(x', R)} \right] \right\}$$

shock index $q = (r + 2)/(r - 1) > \gamma_s$ (bg CR index), and $r = u_1/u_2$, R -particle rigidity, $f_\infty \propto R^{-\gamma_s}$

- **NB: steeper source spectra \rightarrow stronger reacceleration! Recall secondaries**

- κ increases along the CR path, as the turbulence decays.

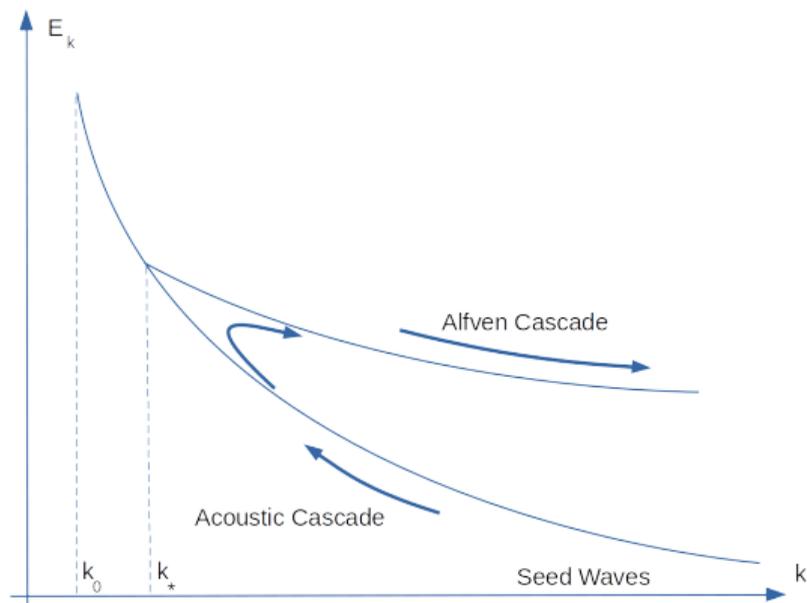
$$\Phi(x, R) = u_1 \int_0^x \frac{dx'}{\kappa(x', R)} \rightarrow \Phi_1 + u \int_{x_0}^\zeta \frac{dx'}{\kappa_{\text{prop}}(x', R)}$$

- it can be shown that the main contribution comes from the second term, $x_0 \rightarrow 0$. With lateral particle losses from the flux tube added, $\Phi(R)$ takes the form (MM & I.Moskalenko, ApJ '21,22)

$$\Phi(R) = (R_0/R)^a + (R/R_L)^b, \quad a = 2 - q_{\text{turb}}, \quad b = q_{\text{turb}} - 1$$

The 10-TV bump results from a local elevation of the CR spectrum by reacceleration and convecting CRs with $R \lesssim 1$ TV away with the ISM flow

Turbulent Cascades: What to plug in as q_{turb} ?



- acoustic waves steepen into shocks, and the acoustic cascade is fully determined by ∇P_{CR}
- ∇P_{CR} drives shock merger, @ γ_D -rate

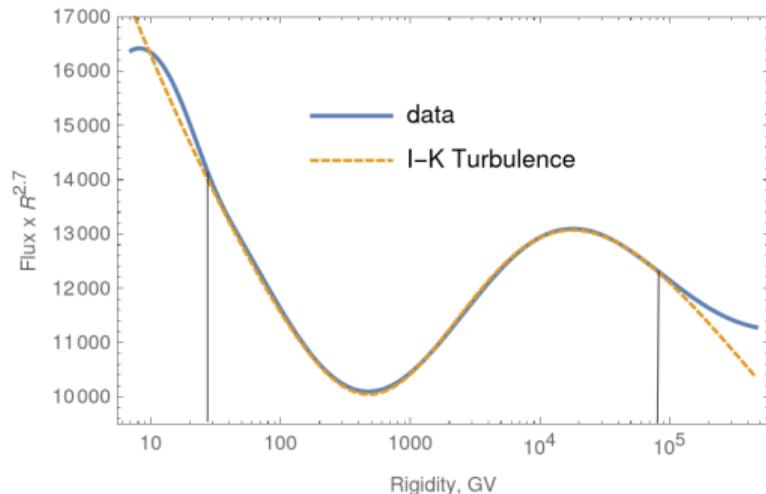
$$E_k^s = \frac{2\pi^2}{3(\gamma + 1)^2 \rho_0^2 C_s^2} \left(\frac{\partial \bar{P}_{\text{CR}}}{\partial r} \right)^2 \cdot \frac{1}{k^3} = \frac{\gamma_D^2}{k^3}$$

- acoustic inverse cascade is intercepted by direct Alfvénic cascade

- acoustic cascade starts from short MS seed waves, resonantly driven by CR anisotropy

$$E_k^A \sim \frac{\sqrt{\gamma_D} V_A^{3/2}}{k^{3/2}} \propto \frac{\delta B_k^2}{B^2}, \quad \rightarrow a = \frac{1}{2}$$

Spectrum Fit: Idealized Data (no errors)



$$f_s(R) = A_s R^{-\gamma_s} \left\{ 1 + \frac{\gamma_s + 2}{q - \gamma_s} \exp \left[- \left(\frac{R_0}{R} \right)^a - \left(\frac{R}{R_L} \right)^b \right] \right\}$$

- Parameter R_0 can be related to CR pressure and flux tube size, l_{\perp} (loss-free fit, $R_L = \infty$ here)

- use synthetic data from [Boschini+, ApJ 2020](#) (analytic curve, demodulated)
- we know $a = b = 1/2$ (IK-spectrum), and find R_0 , $K = (\gamma_s + 2) / (q - \gamma_s)$ from the fit.

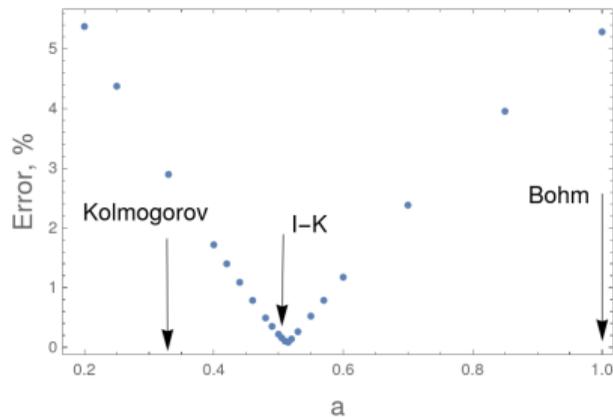
$$\sqrt{R_0} \simeq \frac{3u}{c\sqrt{r_{GV}l_{\perp}}} \int_0^{\zeta_{\text{obs}}} \sqrt{\frac{P_{\text{CR}}}{\rho C_s V_A}} dz$$

- K defines Mach number, M ; R_0 relates the distance ζ_{obs} to l_{\perp} , here $r_{GV} \equiv r_g$ (1GV)
- from the best fit we find $a = 0.515$, $K = 2.39$, $R_0 = 4434 \text{ GV}$.

$$M = 1.55, \quad \frac{\zeta_{\text{obs}}}{\sqrt{r_{GV}l_{\perp}}} \approx 2.2 \cdot 10^2 \frac{c}{u} \sqrt{\frac{\rho C_s V_A}{P_{\infty}}}$$

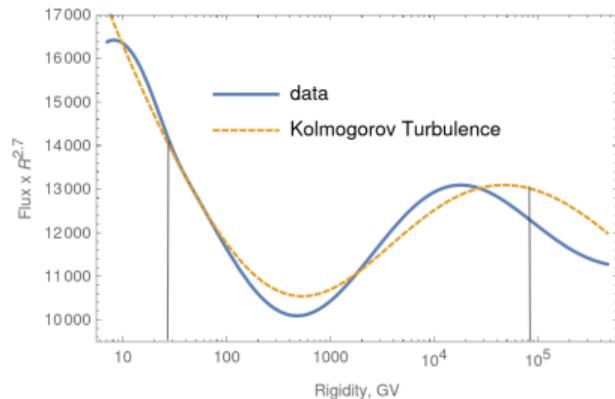
MM & I. Moskalenko, ApJ '21, 22

Unknown Problem Parameters Inferred from best Fit



- **nominal value** for $a = 1/2$ (Iroshnikov-Kraichnan)
- best fit value $a = 0.515$, rel. error $\Delta \approx 9.1 \cdot 10^{-4}$

$$\Delta = \int_{R_1}^{R_2} |f - f_d| dR \Big/ \int_{R_1}^{R_2} f_d dR$$

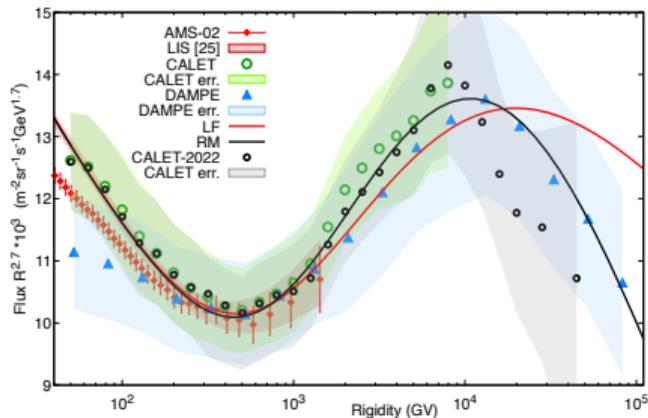


- Parameters inferred from the fit
 - Mach number: $M = 1.55$
 - reaccelerated CRs/background ratio: $K = 2.4$
 - Distance -size relation $\zeta_{\text{obs}}[\text{pc}] \sim 10^2 \sqrt{l_{\perp} [\text{pc}]}$

Spectrum Fit: Real Data adjusted for systematic errors

Parameter (St. err. %)	$R_0(\text{GV})$	$R_L(\text{GV})$	q	$K = (\gamma + 2)/(q - \gamma)$	χ^2_{\min}/dof	dof
Realistic model (RM)	5878 (3.5%)	2.24×10^5 (28%)	4.2	3.59 (4.9%)	0.10	76-3
Loss-free model (LF)	4795 (3.2%)	∞	4.7	2.58 (2.9%)	0.19	76-2

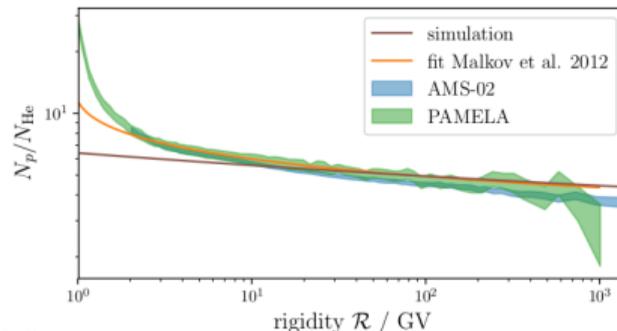
- data benchmarked by spectral minima to demodulated AMS-02 data of [Boschini+ ApJ 2020](#)
- $R = \tilde{R}/1.12$, Flux = $\tilde{\text{Flux}} \times 1.09$ -CALET
- $R = \tilde{R}/0.95$, Flux = $\tilde{\text{Flux}} \times 0.98$ -DAMPE



MM & Moskalenko, ApJ 2022

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- Using the shock and propagation parameters obtained from the proton fit, (Table) we fit the spectra of other species
- He, C, O and all other SNR-accelerated elements with $\langle A/Q \rangle \approx 2$ have flatter than proton spectra by ≈ 0.1 (MM 1998, MM, Diamond and Sagdeev, Hanusch, Liseykina, MM, 2019)



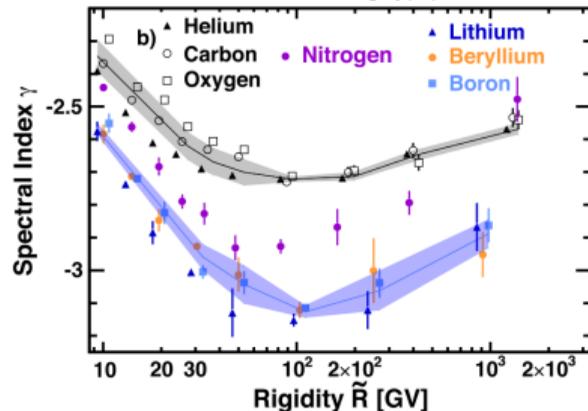
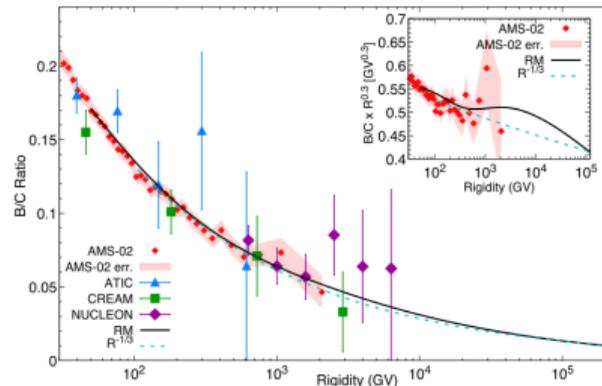
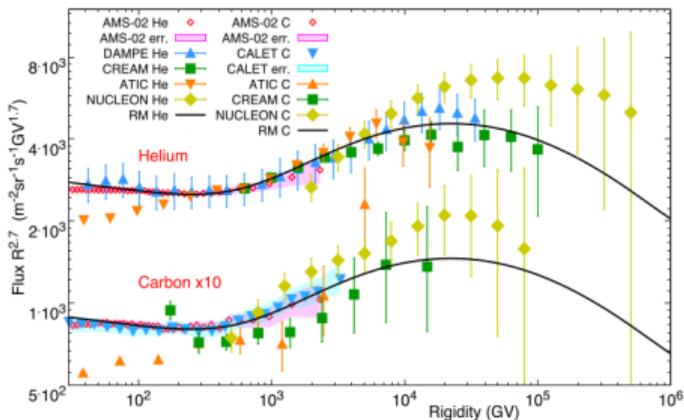
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Spectrum Fit: Secondaries and B/C

$$f_s(R) = A_s R^{-\gamma_s} \left\{ 1 + \frac{\gamma_s + 2}{q - \gamma_s} \exp \left[-\sqrt{\frac{R_0}{R}} - \sqrt{\frac{R}{R_L}} \right] \right\}$$

- q -shock spectral index fixed by the proton fit
- γ_s background spectrum of He and C
- $\gamma_s(\text{proton}) > \gamma_s(\text{He, C}) \rightarrow$ the CR break is less pronounced for He, C
- $\gamma_s(B, Be, Li) > \gamma_s(p) \rightarrow$ CR break is stronger

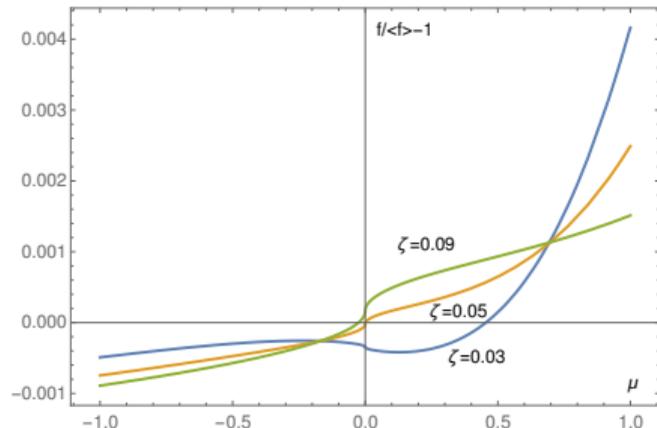


Small-Scale Anisotropy: FP Solution vs. Observations

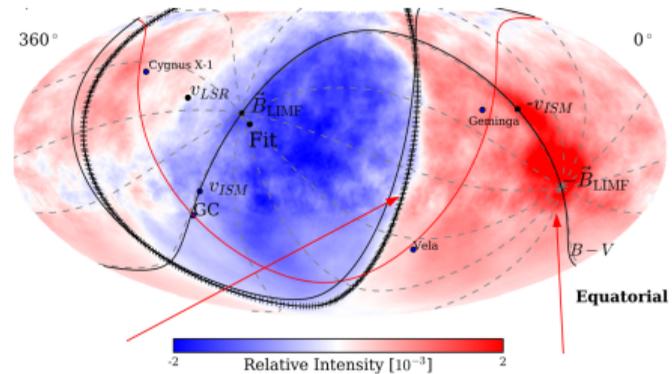
- FP Dominant terms: **prediction**

$$f(\zeta, \mu) = \sum_{n=0}^{\infty} C_n f_n(\mu \cdot \text{sgn}\zeta) e^{-\lambda_n |\zeta|} \quad n = 0, 1$$

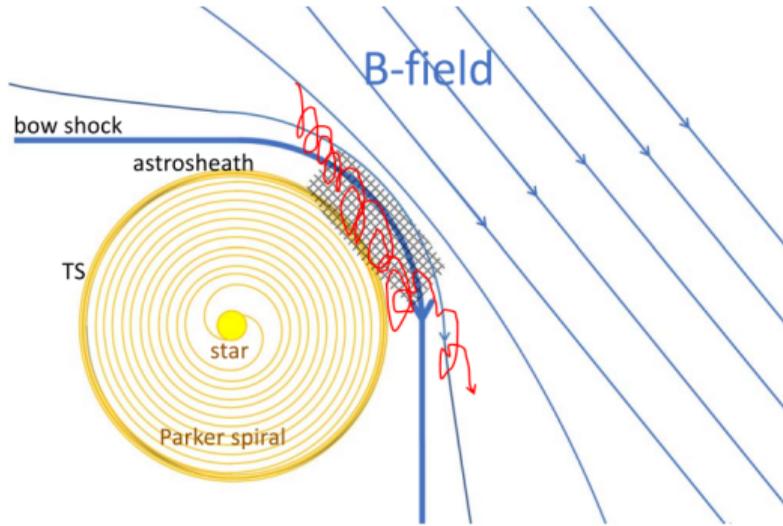
- Eigenvalues λ_n rapidly increase with $n > 0$:
 $\lambda_0 \approx 2\sqrt{5\nu_{\perp}} \ll 1$, $\lambda_{n>0} \sim 10^2(\nu_{\perp}$ lateral losses from the flux tube)
- More subtle anisotropy effects associated with the turbulence spectrum (IK), see [MM & Moskalenko, ApJ '21](#)



- Observations** (Abeysekara+ 2019)
- two key signatures consistent with $\zeta \approx 0.05$ distance predictions:
 - jump across magnetic horizon $\mu \approx 0$
 - enhancement in the field direction $\mu \approx 1$



Bowshock -Termination Shock Reacceleration Mechanism



- Likely object: ϵ -Eri star, 3.2 pc of the Sun, $\dot{M} > 30 \dot{M}_{\odot}$, 10^4 au astrosphere, $\lesssim 7^\circ$ - magnetic connectivity with the Sun

- Space between TS and BS is overpressured by reaccelerated CRs
 - thermal plasma with frozen in B-field is partially expelled
 - magnetic bottle forms
 - ▶ CRs are trapped and can be accelerated more efficiently being trapped between the termination- and bowshock
- Acceleration mechanism - work in progress (MM&M.Lemoine, PRE 2023, MM&I.Moskalenko, ApJ 2022)

Conclusions

- High-precision data on primaries and secondaries CRs around the 10-TeV bump, including angular distributions, can be explained assuming:
 - Sun is crossing a magnetic flux tube filled with reaccelerated CRs
 - ϵ -Eridani (Ran) star is the primary candidate for the CR bump because of its exceptional magnetic connectivity with the heliosphere, large astrosphere, and powerful stellar wind
- Iroshnikov-Kraichnan MHD turbulence, driven by the CR-bump overpressure, is derived and required to fit the data
- Sharp increase of the bump CR intensity across magnetic horizon derived from IK
 - it indicates no CR mirroring \rightarrow incompressible turbulence
- earlier CR bump position: 240 GV (ATIC, Pamela, 2006-2010) \rightarrow 450 GV (current) may point to a time variability, not the calibration issues
- time dependence at 10-30 years suggested
- small-scale anisotropy: key CR diagnostics for the years to come