SOL Broadening by Edge Turbulence: Experiment and Theory of Entrainment Dynamics: from Goldston to Goldenfeld...

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Outline

- Brief Primer on the Edge and SOL, Some History
- SOL Width Problem and the Physics of the Plasma Boundary Layer
- Turbulence Production Ratio and its Implications → Some Data
- Calculating the Scale of the Spreading-Driven SOL → Some Theory
- A Closer Look at Turbulence Spreading → More Theory
- Open Issues and Future Plans

Primer (Brief)

All confinement devices have an <u>edge</u> and SOL (scrape-off layer)

B-SOL

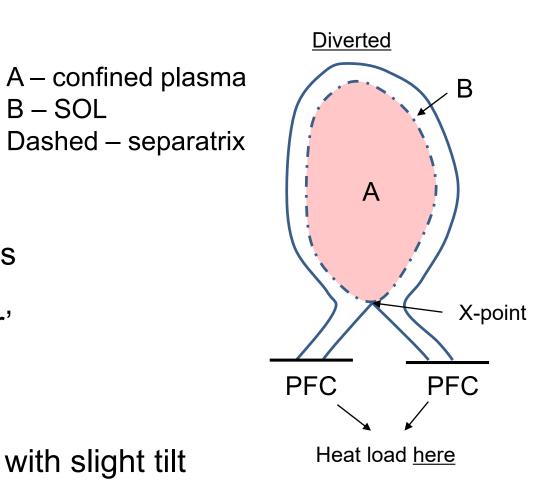
Fueling at Edge

Define:

Confined plasma boundary

- Connection to plasma facing components
- SOL as confined plasma 'boundary layer'

NB: Magnetic field lines are perp to plane, with slight tilt

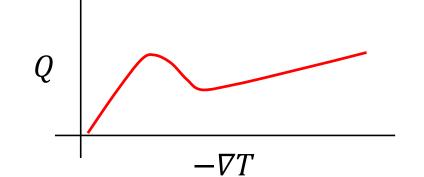


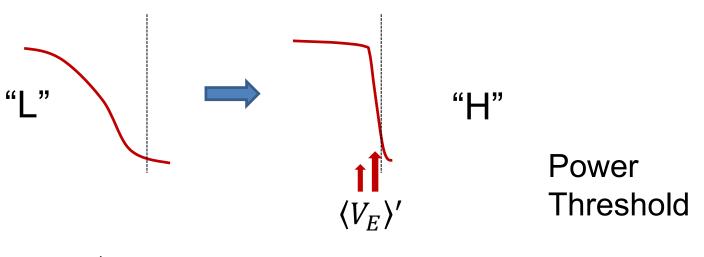
Primer, cont'd

L-H

Key:

- Edge shear layer $\langle V_E \rangle'$ →
- Turbulence quench →
- Transport bifurcation
- Pedestal formation





• Pedestal profiles + δW \rightarrow Edge Localized Modes via Peeling-Ballooning

Primer, cont'd

• SOL: $\nabla \cdot \vec{\Gamma} = \nabla \cdot \vec{Q} = 0$ (open lines)

$$\Gamma_{\perp} \approx -D\partial_r n$$
 (?) $\nabla_{\perp} \sim \partial_r \sim 1/\lambda_{\perp}$

$$\nabla_{\perp} \sim \partial_r \sim 1/\lambda_{\perp}$$

$$\Gamma_{\parallel} \approx \alpha c_s n$$

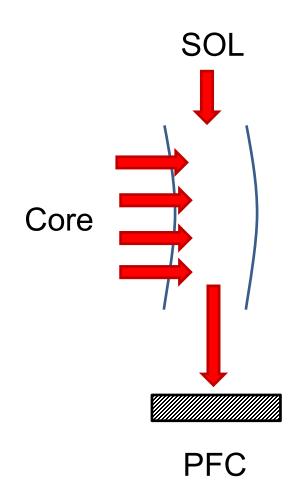
$$V_{\parallel} \sim 1/L_c \sim 1/Rq$$

$$\rightarrow D \partial_r^2 n \sim \alpha n/L_c$$

$$\tau_{\parallel} \approx Rq/c_s$$

$$\lambda_{\perp} \sim (D\tau_{\parallel})^{1/2} \sim \text{crude SOL width}$$





Cynic's History of MFE

- Mid-50's: MCF declassified
- Mid-60's: Trieste → basic tokamak theory
- Mid-70's: PLT NBI → PPPL declares victory (Furth)
- Late 70's-80's: Wait a sec... τ_E degrades with ↑ P_{in} !?
 (Rebut, Furth, Okawa....)
- '82 →: L→H transition discovered on ASDEX (F. Wagner)
 - Spontaneous transition to high confinement, Edge transport barrier
 - ELM's discovered

Key: Boundary Control - Divertor





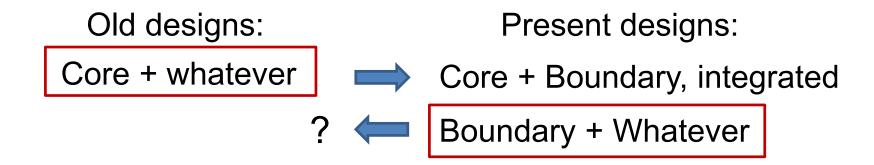
This way to Waterloo

History, cont'd

- '90's → ITB's → evolutionary dead end ?!
- 2000 → Rising concern about ELM and PFC issues, re: ITER
- 2012: Labombard scaling studies + Goldston HD model $\rightarrow \lambda_q \sim 1/B_\theta \rightarrow$ larminar plasma boundary layer too narrow \rightarrow enter the heat load problems
- 2013: Kikuchi TTF Talk (Sonoma)
 - Conflict between good confinement and good power handling
 - "Kill H-mode" (?...)

History, cont'd

- Present Day:
 - Trade offs between confinement and power handling → center stage
 - Enhanced confinement + turbulent edge:
 - Grassy ELMs, WPQHM, I-mode, RMP, Negative Triang., ...
 - ITB + L-mode edge, ITB + R.I. ? Staircase+ ???
 - Divertors + Detachment, Density Limit



History, Summary

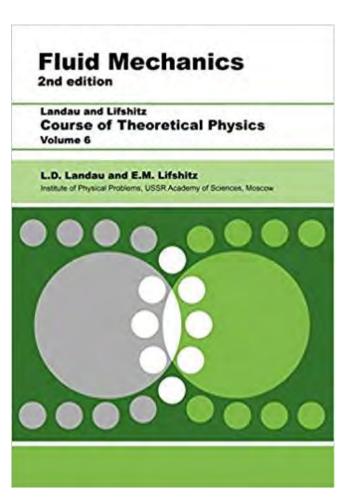
Edge + Boundary Physics has been the center of the action in MFE since 1980's

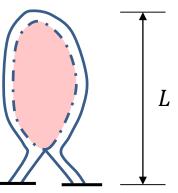
Background

Conventional Wisdom of SOL:

(cf: Stangeby...)

- Turbulent Boundary Layer, ala' Blasius, with D due turbulence
- $-\delta \sim (D\tau)^{1/2}$, $\tau \approx L_c/V_{th}$
- $D \leftrightarrow$ local production by SOL instability process
 - → familiar approach, D ala' QL
- Features:
 - Open magnetic lines → dwell time τ limited by transit,
 conduction, ala' Blasius
 - Intermittency → "Blobs" etc. Observed. Physics?



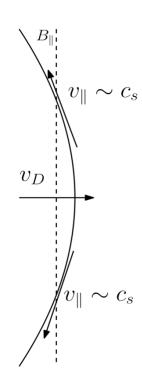


Background, cont'd

But... Heuristic Drift (HD) Model (Goldston +)

$$- \ V \sim V_{\rm curv} \ , \ \tau \sim L_c/V_{thi} \ , \ \lambda \sim \epsilon \ \rho_{\theta i}$$
 \rightarrow SOL width

- Pathetically small
- Pessimistic B_{θ} scaling, yet high I_p for confinement
- Fits lots of data.... (Brunner '18, Silvagni '20)



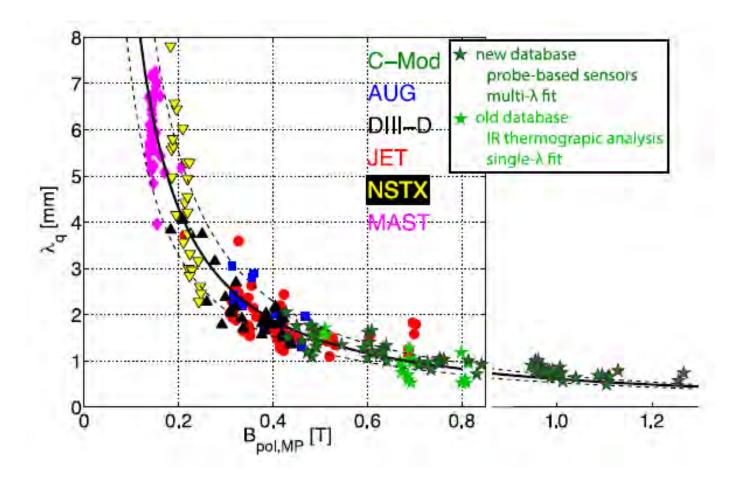
Why does neoclassical work? → ExB shear suppresses SOL modes i.e.

$$\gamma_{\text{interchange}} \sim \frac{c_s}{(R_c \lambda)^{\frac{1}{2}}} + \frac{3T_{edge}}{|e| \lambda^2}$$

shearing $\leftarrow \rightarrow$ strong λ^{-2} scaling

from:
$$\frac{c_S}{(R_C\lambda)^{\frac{1}{2}}} - \langle V_E \rangle'$$

Background: HD Works in H-mode



HD is Bad News...

Background, cont'd

THE Existential Problem... (Kikuchi, Sonoma TTF):

Confinement \rightarrow H-mode $\leftarrow \rightarrow$ ExB shear

Desire Power Handling \rightarrow broader heat load, etc $\rightarrow \underline{\text{Both}} \text{ to be good } !$

How reconcile? – Pay for power mgmt with confinement ?!

- Spurred:
 - Exploration of turbulent boundary states with improved confinement: Grassy ELM, WPQHM,
 I-mode, Neg. D ... N.B. What of ITB + L-mode edge?
 - SOL width now key part of the story
 - Simulations, Visualizations (XGC, BOUT...) ~ "Go" to ITER and all be well
- But... What's the Physics ?? How is the SOL broadened?

SOL Boundary Layer:

Turbulence Production Rate and

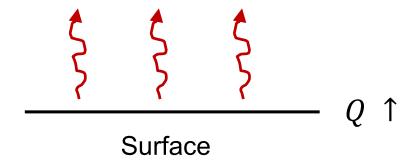
the Role of Spreading

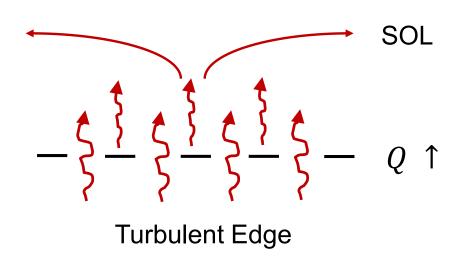
SOL BL Problem

- Classic flux-driven BL problem
 - Heat flux at surface drives
 - Production = gQ $\tilde{V}_E \sim (gQz)^{1/3}$ etc
 - Plumes

Adapt to SOL?

- SOL
 - Open field lines
 - Turbulent energy flux and heat flux, etc drive
 - Turbulence spreading (Garbet, P.D., Hahm, …)
 - Includes 'blobs' c.f. Manz, 2015





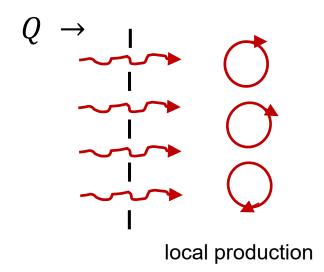
SOL BL Problem

SOL Excitation

- Local production (SOL instabilities)
- Turbulence energy influx from pedestal

Key Questions:

- Local drive vs spreading ratio $\rightarrow Ra$
- Is the SOL usually dominated by turbulence spreading?
- How far can entrainment penetrate a stable SOL → SOL broadening?
- Effects ExB shear, role structures ?



Physics Issues – Part I

- Measure and Characterize Turbulence Energy Flux at LCFS
- Determine Relative Contributions of :
 - Influx/Spreading thru LCFS
 - SOL Production

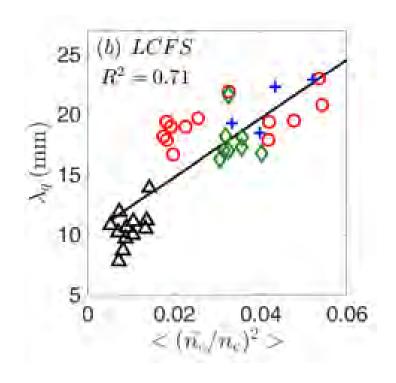
 $R_a \rightarrow \text{Production Ratio}$

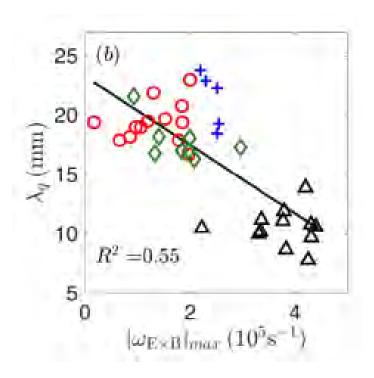
- Trends in λ_a and R_a vs : ExB shear, 'Blob' Fraction...
- Question: To what extent is SOL turbulence usually spreading driven?
- → Phenomenology... (see Ting Wu +, submitted 2022)

Experiments and Data Set

- HL-2A limited OH plasmas classic "boring plasmas"
- Reciprocating probe array ←→ Outboard mid-plane
- $q_{\parallel} = \gamma J_{sat} T_e$, $\gamma \equiv$ sheath transmission coefficient
- Database: 'Garden Variety OH' ~ 150 kA, 1.4T
- Similar, with $\lambda_q \gg \lambda_{HD}$, except: black triangles \triangle
 - $-\lambda_q > \lambda_{HD}$, not \gg
 - Significant GAM activity → stronger ExB shear

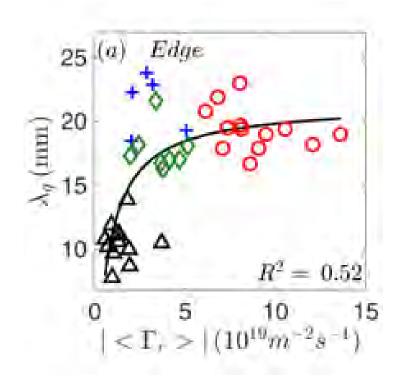
λ_q Trends 1 – Fluctuation Levels and Shearing

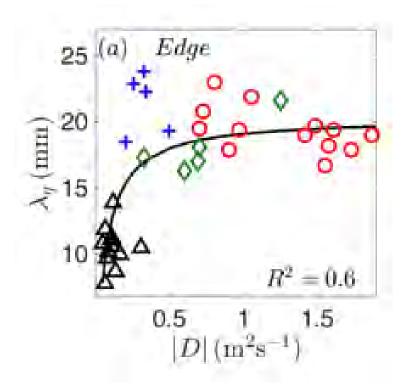




- λ_q increases for increasing fluctuation intensity at <u>lcfs</u>
- λ_q decreases for increasing ExB shear at <u>lcfs</u>
- Max $\omega_{E\times B}$ at shear layer ~ lcfs

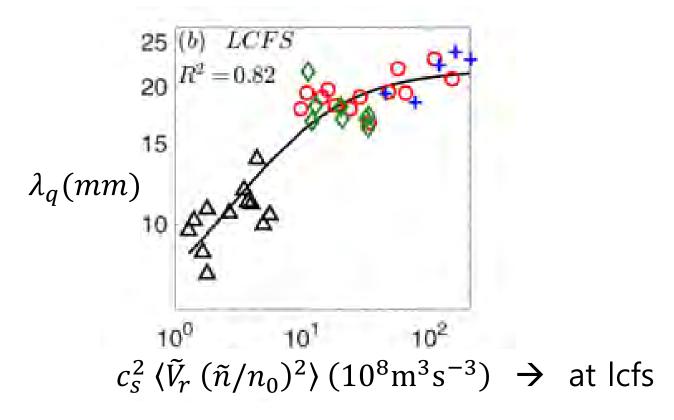
λ_q Trends 2 – Particle Flux and Diffusion





- λ_q increases for increasing <u>edge</u> Γ_n
- λ_q increases for increasing <u>edge</u> D
- ? Saturation might expect $\lambda \sim (D\tau)^{1/2}$ scaling ...

λ_q Trends 3 – Spreading!

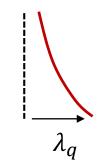


- $\Gamma_{\varepsilon} = c_s^2 \langle \tilde{V}_r (\tilde{n}/n_0)^2 \rangle \rightarrow \text{flux of turbulence internal energy thru lcfs}$
- Direct measurement of <u>local</u> spreading flux
- Consistent with expected trend of expanded SOL width due to increasing spreading across lcfs

SOL Fluctuation Energy – Production Ratio

1 Fluid •
$$\rho\left(\frac{\partial \vec{V}}{\partial t} + \vec{V} \cdot \nabla \vec{V}\right) = -\nabla P + \frac{1}{c} \vec{J} \times \vec{B} + \rho g \hat{r}$$

$$\nabla \cdot \vec{V} = 0, \ \tilde{P} + \frac{\vec{B}_0 \cdot \tilde{B}}{4\pi} \approx 0$$
SOL interchange



•
$$\partial_{t}(KE)_{SOL} = -\int_{0}^{\lambda} dr \, \nabla \cdot \Gamma_{E} + \int_{0}^{\lambda} dr \left[\frac{c_{S}^{2}}{R} \left\langle \frac{\tilde{V}_{r}\tilde{n}}{n_{0}} \right\rangle - \left\langle \tilde{V}_{r}\tilde{V}_{\perp} \right\rangle \frac{\partial}{\partial r} \left\langle V_{\perp} \right\rangle \right]$$

$$= -\Gamma_{E} |_{\lambda_{q}} + \Gamma_{E}|_{1cfs} + [SOL Integrated local production]$$

Fluctuation Energy Influx to SOL

• $\Gamma_E = \langle \tilde{V}_r \tilde{V}^2 \rangle \approx c_s^2 \langle \tilde{V}_r (\tilde{n}/n_0)^2 \rangle \rightarrow$ amenable to measurement Take: KE flux ~ Int. Energy Flux ($\sqrt{}$ for drift-interchange) this gives ...

Aside: On Calculating the Spreading...

- Why perturbed pressure balance?
 - Else, $\langle \vec{V}\cdot \nabla P\rangle$ and $\langle \rho \nabla\cdot \vec{V}\rangle$ enter energy balance. Acoustic energy propagation irrelevant on $\tau\gg au_{MS}$
 - Can eliminate via vorticity eqn, $\vec{V} = \vec{E} \times \vec{B}$ etc.
- Interchange drive: $\kappa P \rightarrow \kappa \langle \tilde{V}_r \tilde{P} \rangle \approx g c_s^2 \langle \tilde{V}_r \tilde{n} \rangle$

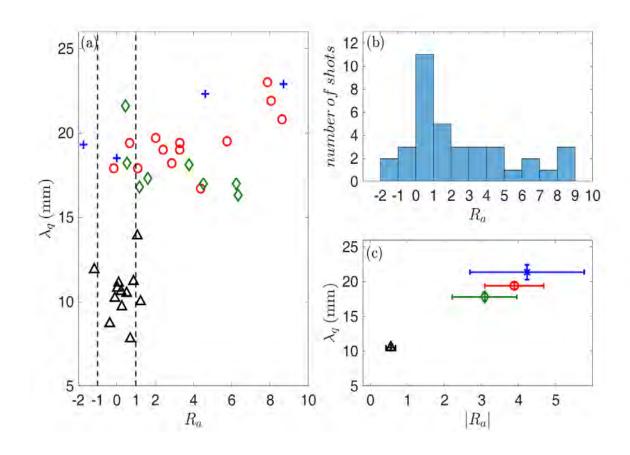
as cannot measure \tilde{P} fluctuations

How important is spreading?

$$R_a = c_s^2 \langle \tilde{V}_r (\tilde{n}/n_0)^2 \rangle \Big|_{\text{lcfs}} / \int_0^{\lambda} dr \frac{c_s^2}{R} \langle \tilde{V}_r \tilde{n}/n_0 \rangle$$

- Ratio of fluctuation energy influx from edge i.e. spreading drive to net production in SOL
- $-R_a < 1 \rightarrow SOL$ locally driven
- $-R_a \gg 1 \rightarrow SOL$ is spreading driven
- Quantitative measurement by Langmuir probes
- N.B. very simple; likely lower bound, as local production smaller

Production Ratio - Measurements



$$R_a = \frac{\text{Fluctuation Energy Influx}}{\text{SOL Local Production}}$$

Observe:

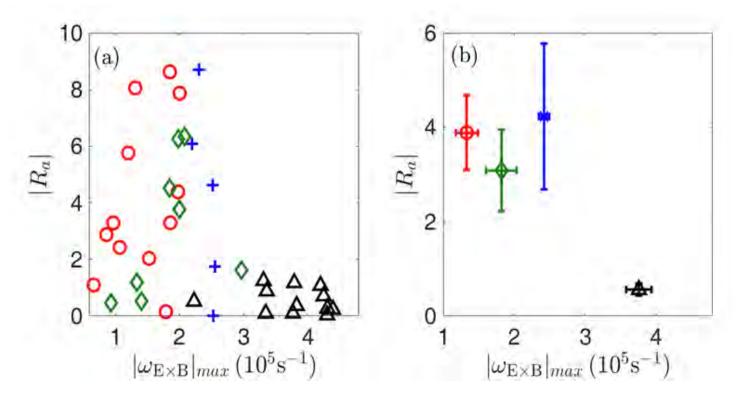
- $-\lambda_a$ increases with R_a
- Most cases $R_a > 1$
- Broad distribution R_a values
- Low R_a values ↔ strong ExB shear
 N.B. Non-trivial, as shear enters production, also via cross phase

Also:

- Some R_a < 0 cases → inward spreading ↔ local measurement trend outward
- Some very large R_a values

What is happening?

Production Ratio vs ExB Shear 1

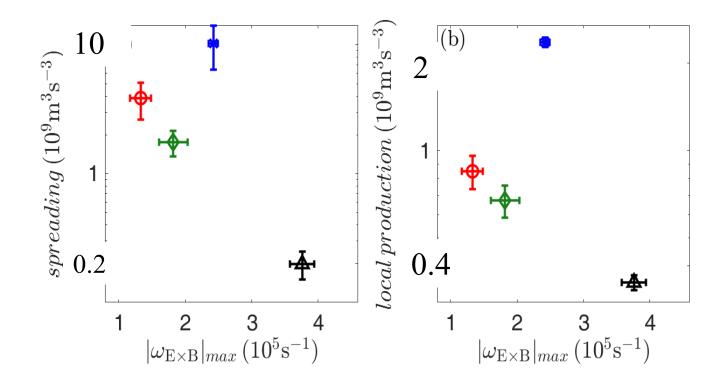


- Low values of $|R_a|$ at high V'_E
- But why?

$$R_a = c_s^2 \langle \tilde{V}_r (\tilde{n}/n_0)^2 \rangle |_{\text{lcfs}} / \int_0^{\lambda} dr \frac{c_s^2}{R} \langle \tilde{V}_r \tilde{n}/n_0 \rangle$$

- → Expect shear inhibits both spreading and transport flux?
- ←→ ExB shear enters phase relation in both

Production Ratio vs ExB Shear, cont'd



- Both spreading and local production drop due high V_E'
- But spreading x (1/10) vs Production x (1/2)
- \rightarrow Spreading flux significantly more sensitive to V'_E than transport flux
- ←→ Triplet vs quadratic → Phases?

Large $R_a \rightarrow \text{'Blobs'}$?!

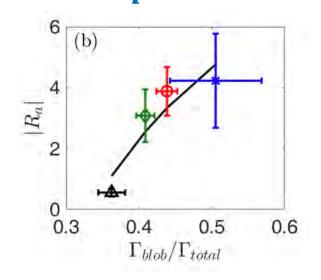
- What of the large R_a values?
- Suspect Structure Emission i.e. "blobs" !?
- Test:
 - Conditional averaging (i.e. threshold $\tilde{n} > 2\tilde{n}_{rms} \rightarrow$ "blob")
- R_a 2-1 0 1 2 3 4 5 6 7 8 9 10 R_a Physics of the "2" ?

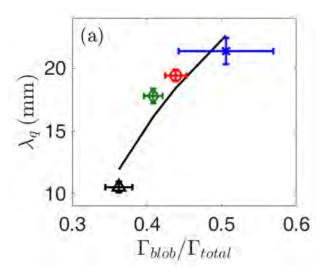
- Threshold arbitrary → setting based upon previous studies
- Compute R_a , Γ etc. with conditionally averaged quantities

Especially: $\Gamma_{blob} / \Gamma_{total}$

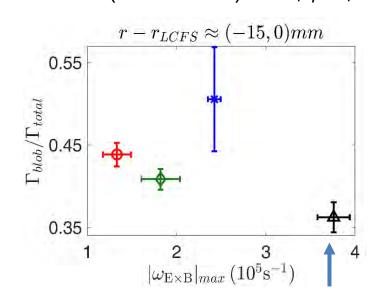
Flux carried by "blobs"

Large $R_a \rightarrow \lambda_q$ increases with 'blob' fraction





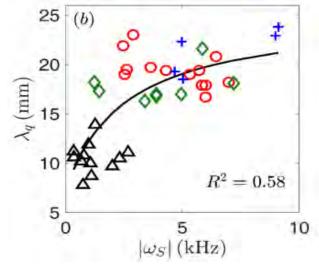
- Large R_a cases \longleftrightarrow larger 'blob fraction' of flux \longleftrightarrow spreading encompasses 'blobs' (c.f. Manz +) \to $\langle \tilde{V}_r \tilde{n}^2 \rangle$
- λ_q increases with Γ_b/Γ_{Tot}

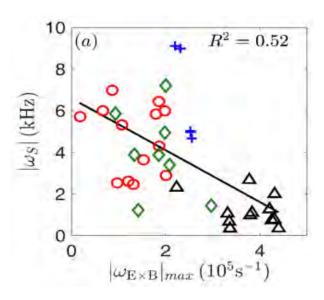


 High ExB shear cases → low 'blob' fraction (Consistent with Bodeo+, '03)

Time Scales

- Spreading rates: $\omega_S \approx -\partial_r \langle \tilde{V}_r \tilde{n} \tilde{n} \rangle / \langle \tilde{n}^2 \rangle$ characteristic rate of spreading (Manz +)
- Shearing rate V'_E





- λ_q broadens for large ω_s
- Stronger shear reduces spreading rate

Partial Summary

- Significant, mostly outward, spreading measured at lcfs
- Identified and calculated production ratio

```
R_a = \text{(spreading influx) / (local production)}
```

- Most cases: $R_a > 1$ spreading dominant player in SOL energetics
- ExB shear reduces $R_a \leftarrow \Rightarrow$ spreading more sensitive to V_E' than transport and production phases ?
- High R_a spreading $\leftarrow \rightarrow$ 'blob' dominated dynamics \rightarrow how calculate?

YES → SOL turbulence usually spreading driven!

"The conventional wisdom is little more than convention" - JKG

N.B. No use of closure of spreading flux

Calculating the Width of the Spreading-Driven SOL

Physics Issues – Part II

- How <u>calculate</u> SOL width for turbulent pedestal but a locally stable SOL?
 - spreading penetration depth
 - must recover HD in WTT limit
- \rightarrow Scaling and cross-over of λ_q relative HD model
- What is effect/impact of barrier on spreading mechanism?
 - Can SOL broadening and good confinement be reconciled?

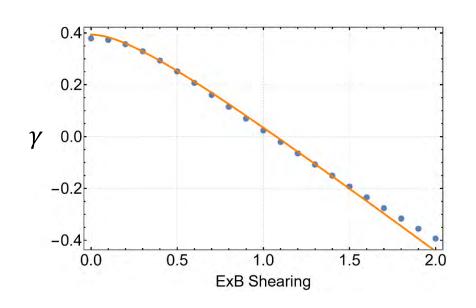
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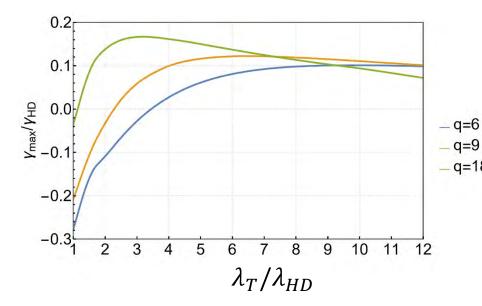
Simulation inadequate!

Need more than color pictures...

Model 1 – Stable SOL – Linear Theory

 Standard drift-interchange with sheath boundary conditions + ExB shear (after Myra + Krash.)





Maximal Linear Growth Rate of Interchange Mode in the SOL v.s. normalized layer width λ_D/λ_{HD} at different SOL safety factor q (with $\beta=0.001$)

Linear Growth Rate of a specific mode (fixed k_y) v.s. $E \times B$ shear at $q = 5, \beta = 0.001, k_y \cdot \lambda_{HD} = 1.58$.

- Relevant H-mode ExB shear strongly stabilizing $\gamma_{HD} = c_s/(\lambda_{HD}R)^{1/2}$
- Need λ/λ_{HD} well above unity for SOL instability. $V_E' \approx \frac{3T_e}{|e|\lambda^2} \rightarrow$ layer width sets shear

Model 2 – Two Multiple Adjacent Regions

"Box Model" – after Z.B. Guo, P.D.

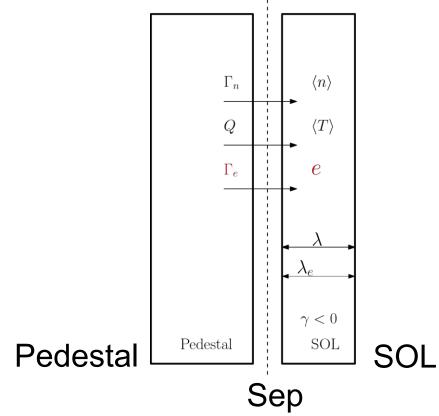


Illustration of Two Box Model: SOL driven by particle flux, heat flux and intensity flux (Γ_e) from the pedestal. The horizontal axis is the radial direction, and vertical axis is the poloidal direction.

- Key Point:
 - Spreading flux from pedestal can enter stable SOL
 - Depth of penetration → extent of SOL broadening
 - → Problem in one of entrainment/penetration

Width of Stable SOL

• Fluid particle: $\frac{dr}{dt} = V_{Dr} + \tilde{V}_{Dr}$ • Dwell time: τ_{\parallel}

$$\delta^2 = \langle \left(\int \left(V_D + \tilde{V} \right) dt \right) \left(\int \left(V_D + \tilde{V} \right) dt \right) \rangle$$

$$\langle (\text{step})^2 \rangle = V_D^2 \tau_\parallel^2 + \langle \tilde{V}^2 \rangle \tau_c \tau_\parallel$$

$$= \lambda_{HD}^2 + \varepsilon \tau_\parallel^2$$

$$\text{correlation time modest turbulence }$$

$$\text{turbulence energy density}$$

$$\text{correlation time modest turbulence}$$

$$\text{i.e. drift + diffusion}$$

- So $\lambda = \left[\lambda_{HD}^2 + \varepsilon \tau_{\parallel}^2\right]^{1/2} \rightarrow \underline{SOL \ width}$ [Effects add in quadrature]
- How compute ε ? \rightarrow turbulence energy!

Calculating the SOL Turbulence Energy 1

- $K \epsilon$ type model, mean field approach (c.f. Gurcan, P.D. '05 et seq)
 - Can treat various NL processes via σ , κ
 - Exploit conservative form model
- $\partial_t \varepsilon = \gamma \varepsilon \sigma \varepsilon^{1+\kappa} \partial_x \Gamma_e$ Spreading, turbulence energy flux Growth $\gamma < 0$ NL transfer $\gamma_{NL} \sim \sigma \varepsilon^{\kappa}$ here contains shear + sheath
- N.B.: No Fickian model of Γ_e employed
- Readily extended to 2D, improved production model, etc.

Calculating the SOL Turbulence Energy 2

- Integrate ε equation \int_0^{λ}
- Take quantities = layer average

•
$$\Gamma_{e,0} + \lambda_e \gamma \varepsilon = \lambda_e \ \sigma \ \varepsilon^{1+\kappa}$$

Separatrix fluctuation energy flux ——

Single parameter characterizing spreading

So for
$$\gamma < 0$$
,

$$\Gamma_{e,0} = \lambda_e |\gamma| \varepsilon + \sigma \lambda_e \varepsilon^{1+\kappa}$$

 $\Gamma_{e,0}$ vs linear + nonlinear damping

$$\lambda_e$$
 = layer width for ε

Calculating the SOL Turbulence Energy 3

[Mean Field Theory]

Full system:

$$\Gamma_{e,0} = \lambda_e |\gamma| \varepsilon + \sigma \lambda_e \varepsilon^{1+\kappa}$$

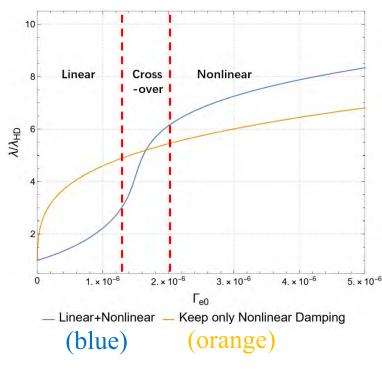
$$\lambda_e = \left[\lambda_{HD}^2 + \varepsilon \tau_{\parallel}^2\right]^{1/2}$$

Simple model of turbulent SOL broadening

- $\Gamma_{0,e}$ is single control parameter characterizing spreading
- $\tilde{\Gamma}_{0,e}$? Expect $\tilde{\Gamma}_e \sim \Gamma_0$

SOL width Broadening vs $\Gamma_{e,0}$

SOL width broadens due spreading



 λ/λ_{HD} plotted against the intensity flux Γ_{e0} from the pedestal at $q=4,\beta=0.001,\kappa=0.5,\sigma=0.6$

Variation indicates need for detailed scaling analysis

- Clear decomposition into
 - Weak broadening regime → shear dominated
 - Cross-over regime
 - Strong broadening regime
 - → NL damping vs spreading

relevant

• Cross-over for:

$$\langle \tilde{V}^2 \rangle \sim V_D^2 \implies$$
 cross-over $\Gamma_{0,e}$

• Cross-over for $\tilde{V} \sim O(\epsilon)V_*$

- Need consider pedestal to actually compute $\Gamma_{e,0}$
- Two elements

Separatrix $\Gamma_e = -\tau_c K \partial_x K$ Intensity Profile

Does another trade-off loom?

- -- Pedestal Turbulence: Drift wave? Ballooning?
- -- Effect of transport barrier ←→ ExB shear layer → barrier permiability!?
- Key Point: shearing limits correlation in turbulent energy flux

i.e.
$$\Gamma_{e,0} \approx -\tau_c \, I \, \partial_x \, I \approx \tau_c \, I^2 \, / w_{\rm ped}$$
 (Hahm, PD +) ped turbulence correlation time \rightarrow strongly sensitive to shearing intensity

N.B. Caveat Emptor re: intensity flux closure!

Familiar analysis for $D \rightarrow Kubo$

$$D = \int_0^\infty d\tau \, \langle V(0)V(\tau) \rangle = \int_0^\infty d\tau \, \sum_k \left| \tilde{V}_k \right|^2 \exp\left[-k_y^2 \omega_s^2 D \tau^3 - k^2 D \tau \right]$$

• Strong shear (relevant) $au_c = au_t^{1/2} \omega_s^{-1/2}$

$$\tau_c = \tau_t^{1/2} \omega_s^{-1/2}$$

$$\tau_t \sim 1 / k\tilde{V}, \quad \omega_s \sim V_E'$$

Here, via RFB
$$\rightarrow \omega_S = \partial_r \frac{\nabla P_i}{n|e|} \sim \frac{\rho^2}{w_{ped}^2} \Omega_{ci}$$

- $\tau_c + w_{ped}$ + turbulence intensity in pedestal gives $\Gamma_{e,0} \approx \tau_c I^2/w_{ped}$
- Need $\Gamma_{e,0} \ge \Gamma_{e,\min} \approx |\gamma| \lambda_{HD}^3 \tau_{\parallel}^{-2}$

- Pedestal → Drift wave Turbulence
- Necessary turbulence level:

- Weak Shear
$$\frac{\delta V}{c_s} \sim \left(\frac{\rho}{R}\right)^{1/2} q^{-1/4}$$

- Strong Shear
$$\frac{\delta V}{c_S} \sim \left(\frac{\rho}{R}\right)^{1/2} q^{-1/4} \left(\frac{w_{ped}}{\rho}\right)^{-1/8}$$

blue – all damping orange – nonlinear only

0.01

0.02

0.03

 $e\delta\phi/T$

0.04 0.05

- $\rightarrow \lambda/\lambda_{HD}$ vs $|e|\hat{\phi}/T_e$ in pedestal
- \rightarrow ρ/R is key parameter
- Broadens layer at acceptable fluctuation level

green – linear only

- Pedestal → Ballooning modes → Grassy ELMs
- Necessary relate turbulence to $L_{P,crit}$ / L_P 1
- Strong shear:

$$\frac{L_{P_c}}{L_P} - 1 \sim \left(\frac{q\rho}{R}\right)^{\frac{10}{7}} \left(\frac{R}{w_{ped}}\right)^{\frac{16}{7}} \left(\frac{w_{ped}}{\Delta_r}\right)^{\frac{16}{7}} \beta$$

• Supercriticality scales with $\frac{\rho}{R}$, β_t

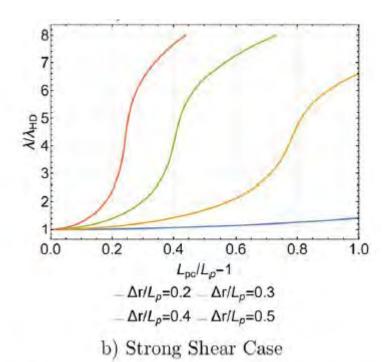


Figure 10. Typical cases for ballooning. The normalized pedestal width $\lambda/\lambda_{\rm HD}$ is plotted against supercriticality $L_{\rm pc}/L_{\rm p}-1$ at different mode width $\Delta/L_{\rm p}$.

Computing the Turbulence Energy Flux 5 → Bottom Line

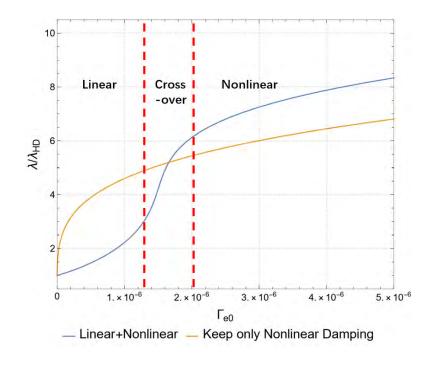
- SOL broadening to $\lambda > \lambda_{HD}$ achieveable at tolerable pedestal fluctuation levels
- DW levels scale $\sim \left(\frac{\rho}{R}\right)^{1/2}$
- Ballooning supercritical scale ~ $\left(\frac{\rho}{R}\right)^{10/7} \beta$
- 'Grassy ELM' state promising
- Sensitivity analysis \rightarrow Cross over ε determined primarily by linear damping (shear). Conclusion ~ insensitive to NL saturation

Partial Summary

Turbulent scattering broadens stable SOL

$$\lambda = \left(\lambda_{HD}^2 + \varepsilon \tau_{\parallel}^2\right)^{1/2}$$

Separatrix turbulence energy flux specifies SOL turbulence drive



$$\Gamma_{0,e} = \lambda_e |\gamma| \varepsilon + \lambda \sigma \varepsilon^{1+\kappa}$$

Broadening increases with $\Gamma_{0,e}$ cross-over for $\langle \tilde{V}^2 \rangle \sim V_D^2$

Non-trivial dependence

• $\Gamma_{0,e}$ must overcome shear layer barrier

Yes – can broaden SOL to $\lambda/\lambda_{MHD}>1$ at tolerable fluctuation levels Further analysis needed

Broader Messages

- Turbulence spreading is important even dominant process in setting SOL width. $\Gamma_{0,e}$ is critical element. $\lambda = \lambda(\Gamma_{0,e}$, parameters)
- Production Ratio R_a merits study and characterization
- Spreading is important saturation meachanism for pedestal turbulence
 - Simulation should stress calculation and characterization of turbulence energy flux over visualizations and front propagation studies.
 - Critical questions include local vs FS avg, channels and barrier interaction, Turbulence 'Avalanches'
- Turbulent pedestal states attractive for head load management

Open Issues

- Quantify $\lambda = \lambda \left(\frac{|e|\widehat{\phi}|}{T} \Big|_{ped} \right)$ dependence
- Structure of Flux-Gradient relation for turbulence energy?
 - Phase relation physics for intensity flux? crucial to ExB shear effects
 - Kinetics $\rightarrow \langle \tilde{V}_r \delta f \delta f \rangle$, Local vs Flux-Surface Average, EM
 - SOL Diffusive? → Intermittency('Blob'), Dwell Time?
 - SOL → Pedestal Spreading ? ←→ HDL (Goldston) ?
 - i.e. Tail wags Dog? Both wagging? → Basic simulation, experiment?

Counter-propagating pulses?

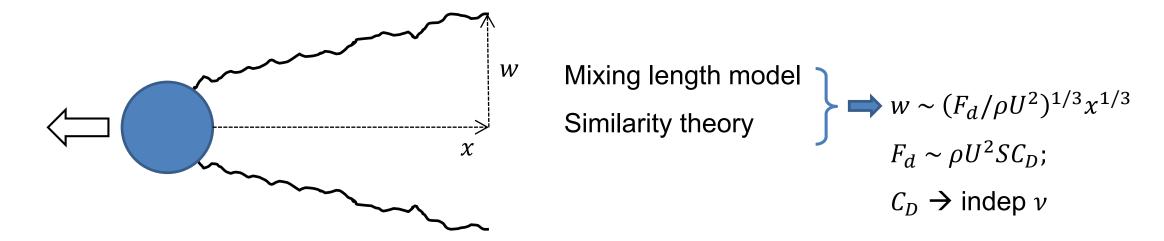
Physics of Turbulence Spreading: General

Perspective

- Structure of the intensity flux-gradient relation(?)
- Spreading as directed percolation...

Spreading: Conventional Wisdom

• Turbulence spreading underpins turbulent wake \rightarrow central example in high Re fluids



• Spreading fundamental to $k - \varepsilon$ type models, as ε evolved as unresolved energy field \rightarrow subgrid models

$$\frac{\partial \varepsilon}{\partial t} + \nabla \cdot (\tilde{V}\varepsilon) + \dots = 0$$
How render tractable

Spreading: cont'd

What you get (usually):

$$\partial_t \varepsilon + \overrightarrow{V}_D \cdot \nabla \varepsilon + \langle \overrightarrow{V}_E(r) \rangle \cdot \nabla \varepsilon - \partial_r D(\varepsilon) \partial_r \varepsilon = P_{src}(\varepsilon) - P_{\text{damp}}(\varepsilon) \rightarrow \gamma(\overrightarrow{x}) \varepsilon$$
drift shear turbulent mixing via closure
$$\gamma = \gamma(\text{gradients, etc})$$

$$D(\varepsilon) \approx D_0 \varepsilon$$
, et. seq. \rightarrow nonlinear diffusion

 $\rightarrow \varepsilon$ evolution as nonlinear Reaction-Diffusion Problem!

(P.D., Garbet, Hahm, Gurcan, Sarazin, Singh, Naulin...)

- Used also in:
 - BLY-style layering models (Ashourvan)
 - 1D L→H models (Miki)

Spreading: cont'd

Spreading as Front → Fast Propagation

i.e.
$$V_f \sim (\gamma D)^{1/2}$$
, etc [N.B. Cahn-Hillard?]

Key component:

$$\nabla \cdot \langle \vec{V} \varepsilon \rangle \rightarrow -\nabla \cdot D(\varepsilon) \cdot \nabla \varepsilon$$
 [Fickian Model]

Expectation: $D(\varepsilon) \sim \chi$, D_n etc. for electrostatic

- Copious simulations: Z. Lin, W.X. Wang, S. Yi, Jae-Min Kwon, Y. Sarazin, ...
 - → Observations, front tracking but critical analysis of model absent ??

No test of Fickian flux model

Experiments: Ancient

Not exactly a new idea ... See Townsend '49 and book

Momentum and energy diffusion in the turbulent wake of a cylinder

By A. A. Townsend, Emmanuel College, University of Cambridge

(Communicated by Sir Geoffrey Taylor, F.R.S.—Received 6 October 1948)

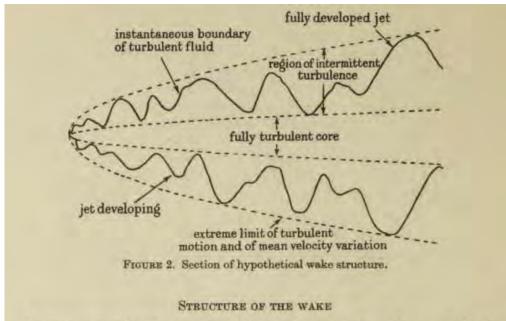
A detailed experimental investigation of the turbulent motion in the wake of a circular cylinder, 0.953 cm. diameter placed in an air-stream of velocity 1280 cm.sec.-1, has been carried out with particular reference to those quantities determining the transport of turbulent energy and mean stream momentum. At distances of 80, 120 and 160 diameters down-stream from the cylinder, direct measurements have been made of mean flow velocity. turbulent intensity, viscous dissipation, energy diffusion, scale, and form factors of the velocity components and their spatial derivatives. These observations show that, except close to the wake centre, the flow at a point fixed with respect to the cylinder is only intermittently turbulent, due to the passage of the point of observation through jets or billows of turbulent fluid emitted from the inner wholly turbulent core of the wake. Further consideration of the results indicates that the turbuleut motion within the jets is solely responsible for the turbulent transfer of momentum, while diffusion of turbulent energy and of heat is carried out by the bulk movement of the jets. Most probably, the jets are initiated by local fluctuations of pressure inside the turbulent core, and in the later stages of their development that are slowed down by adverse pressure gradients. The existence of pressure-velocity correlations of sufficient magnitude is demonstrated by using the equation for the conservation of kinetic energy in the wake, all terms of which are known excepting the one involving the pressure-velocity correlation, which is then obtained by difference. While the conception of

jets of turbulent fluid is more convenient for following the physical processes in the wake, the alternative but equivalent description that the turbulent motion consists of a motion of scale small compared with the mean flow superimposed on a slower turbulent motion whose scale is large compared with the mean flow may be used. A formal explanation of this two-stage turbulent structure in terms of the Fourier representation of the velocity field is suggested, which relates the structure to the presence of a quasi-constant source of energy of meanly fixed wave-number, and to the free boundary which allows an unlimited range of wave-numbers. It is expected that this type of motion will occur in all systems of turbulent shear flow with a free boundary, such as wakes, jets and boundary layers.

→ Wake flow intermittently turbulent

→ Compare transport of momentum and energy (spreading)

Experiments: Ancient, cont'd



Let us now consider the experimental results in turn, and use them to derive information about the detailed properties of these jets of turbulent fluid. In the first place, the velocity product \overline{uv} , representing the Reynolds shear stress, has been measured, and, with the observed distribution of mean velocity across the wake, the effective eddy viscosity ε and the experimental mixing length l may be calculated, using the definitions

$$\overline{uv} = -\epsilon \frac{\partial U}{\partial y}, \quad \epsilon = l\sqrt{v^2}.$$

Experimentally, l is found to be fairly small, approximately 0-07 of the half-width of the mean velocity wake (figure 3), and does not vary greatly over the width of the wake. The small size of l is interpreted as evidence that momentum transfer in the wake is carried out by comparatively small eddies. More significantly, ϵ/γ is not far from constant over the greater part of the wake (figure 4), but this will be discussed later.

→ Wake expansion due jets of expanding fluid

→ Departs mean field theory

→ Mixing length model momentum transport

Experiments: Ancient, cont'd

The product uv may be regarded as the rate of transport of momentum (per unit mass), and similarly the rate of transport of turbulent energy is

$$\frac{1}{3}(\overline{u^2v} + \overline{v^3} + v\overline{w^2}),$$

and, in principle, it is possible to calculate an energy diffusion coefficient δ , analogous with ϵ , by use of the defining equation

$$\overline{u^2v} + \overline{v^3} + \overline{vw^2} = -\delta \frac{\partial}{\partial y} (\overline{u^2} + \overline{v^2} + \overline{w}^2).$$

When this is attempted (figure 5), no simple behaviour is found either for δ , or for the corresponding mixing length. Negative values occur near the wake centre, and, even where the turbulence gradient is fairly uniform, δ remains large compared with ϵ ,

and decreases rapidly with distance from the wake centre. It must be concluded that the use of a diffusion coefficient to describe the transport of turbulent energy is not justified, and that energy diffusion is a process independent of momentum diffusion.

To remove this difficulty, it is not sufficient to consider the effects of intermittency. If the intermittency factor is known, then the mean intensity in the turbulent regions is

$$I_j = \frac{\overline{u^2} + \overline{v^2} + \overline{w^2}}{\gamma},$$

and I_j is found to vary only slightly over the greater part of the wake (figure 6). So a considerable transport of energy is found in the almost complete absence of a real intensity gradient, and it is difficult to see how energy flow can take place by turbulent

movements inside the jets. For the transport mechanism, there is only left the bulk movement of the jets, which is naturally outwards and away from the wake centre. The compensating inflow will consist of non-turbulent fluid transporting no turbulent energy. Consequently, the flow of energy is not dependent on the local intensity gradient (if any), but only on the mean jet velocity and the jet turbulent intensity, which in turn are determined by conditions in the turbulent core.

→ Fickian model for turbulent energy transport

→ "It must be concluded that the use of a diffusion coefficient to describe the transport of turbulent energy is not justified and that energy diffusion is a process independent of momentum diffusion"

Experiments: Modern (Ting Long, SWIP) 1

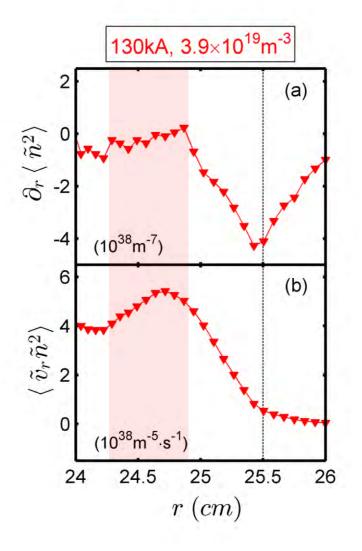
- HL-2A
- Aims:
 - Exploration of intensity flux intensity gradient relation in edge turbulence (exploits spreading, shear layer collapse and density limit studies Long + NF'21)
 - Physics of "Jet Velocity" profile

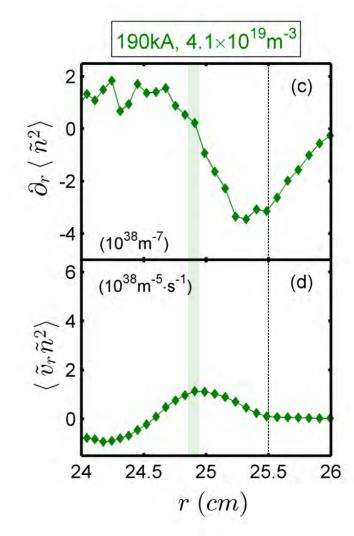
$$V_I = \langle \tilde{V}_r \tilde{n}^2 \rangle / \langle \tilde{n}^2 \rangle$$

N.B. Identified by Townsend

Experiments: Modern 2

• There exits a region in plasma edge, where the turbulence spreading flux $\langle \tilde{v}_r \tilde{n}^2 \rangle / 2$ is large, but the turbulence intensity gradient $\partial_r \langle \tilde{n}^2 \rangle$ is near zero



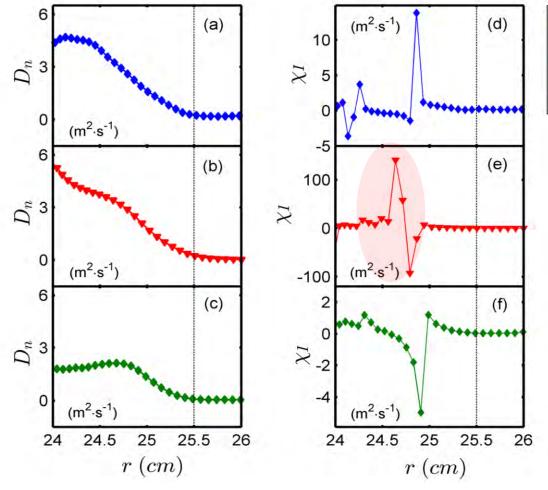


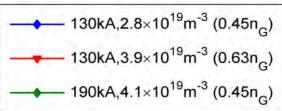
For close \overline{n}_e

- Lower current, width of region is $\sim 5 mm$ $(l_{cr} \sim 4.5 mm)$
- Higher current, width of region is < 1 mm $(\rho_i \sim 0.25 mm)$
- Notice: spreading diffusivity $\chi_I = -\frac{\langle \tilde{v}_r \tilde{n}^2 \rangle}{\partial_n \langle \tilde{n}^2 \rangle}$

Experiments: Modern 3

- Striking difference between particle diffusivity and energy spreading diffusivity
 - ightharpoonup Diffusivity of turbulent particle flux $\langle \tilde{n}\tilde{v}_r \rangle = D_n \partial_r \langle n \rangle$
 - > Diffusivity of turbulence spreading $\langle \tilde{v}_r \tilde{n}^2 \rangle = -\frac{\chi_I}{\partial_r} \langle \tilde{n}^2 \rangle$



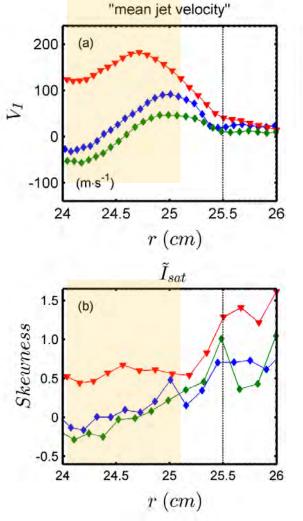


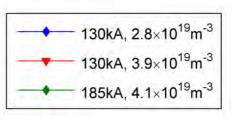
- χ_I is not equal to D_n!
 (in both magnitude and sign)
- χ_I is large where $\partial_r\langle \widetilde{n}^2
 angle$ is near zero
- χ_I increases significantly as \bar{n}/n_G increases (Both \bar{n} and I_p involved)

Practical validity of Fickian model is dubious

Experiments: Modern 4

• The "mean jet velocity" of turbulence spreading $V_I = \frac{\langle \tilde{v}_r \tilde{n}^2 \rangle}{\langle \tilde{n}^2 \rangle}$ and skewness of density fluctuations show strong correlation





- Their trends and signs are consistent
- More work is being done on the correlation between "blobs/holes" and turbulence spreading
- V_I skewness trend follows joint reflection symmetry relation

Spreading as Fluctuation Intensity Pulses

- Edge turbulence intermittent:
 - Strong $\langle V_E \rangle' \rightarrow \sim$ marginal avalanching state
 - Weaker $\langle V_E \rangle' \rightarrow$ 'blobs', etc. $\Gamma_e = \langle \Gamma_e \rangle + \tilde{\Gamma}_e$

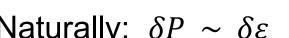
$$\Gamma_e = \langle \Gamma_e \rangle + \tilde{\Gamma}_e$$

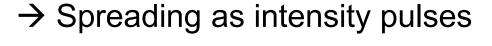
Pulses / Avalanches are natural description

 $\delta P \equiv$ deviation of profile from criticality

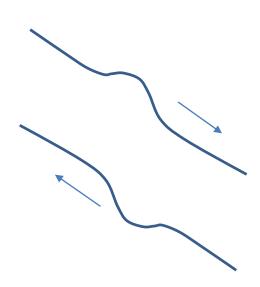
$$\delta P \leftrightarrow (\nabla P - \nabla P_{crit})/P$$

Naturally: $\delta P \sim \delta \varepsilon$





(after Hwa, Kardar, P.D., Hahm)



Pulse, void symmetry arguments etc.

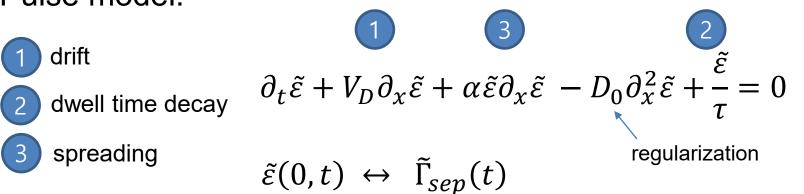
Fluctuation Energy Pulses, cont'd

- Burgers is on the grill...
- New toppings:
 - $-\delta \varepsilon > 0$ turbulence ejected into SOL positive intensity fluctuation
 - $-V_D > 0$ mean drift out curvature
- Scale independent damping
 - $(1/\tau)\delta\varepsilon$ due finite dwell time in SOL \rightarrow order parameter not conserved
 - Noise is b.c.
 - $-\tilde{\Gamma}_{0,e}|_{\text{sep}}$ drives system, space-time

Fluctuation Energy Pulses, cont'd

- Pulse model:

 - spreading



Some limits:

$$-\varepsilon \to 0$$
 , $V_D \partial_{\chi} \tilde{\varepsilon} \sim \frac{\tilde{\varepsilon}}{\tau} \to \lambda \sim \lambda_{HD}$ scale (1 vs 2)

– For ε to matter:

$$\alpha \tilde{\varepsilon} > V_D$$
 \rightarrow amplitude vs neo drift comparison (1) vs (3)

Structure is Burgers + Krook → Crooked Burgers

Fluctuation Energy Pulses, cont'd

Predictions?

Structure formation → Shock Criterion!

i.e. Recall:
$$\frac{d\varepsilon}{dt} = -\frac{\varepsilon}{\tau}$$
 , $\frac{dx}{dt} = \alpha\varepsilon$

Solve via characteristics:

$$x = \alpha \left[z + \frac{\left(1 - e^{-\frac{t}{\tau}}\right)}{(1/\tau)} f(z) \right]$$

Shock for: $f'(z) < -1/\tau$

 \rightarrow inital slope must be sufficiently steep to shock before damped by $1/\tau$

Spreading as Fluctuation Intensity Pulses, cont'd

- $\alpha \frac{\partial \varepsilon}{\partial x}|_{sep} < -\frac{1}{\tau}$ \rightarrow pulse formation criterion \rightarrow intensity gradient

 $\alpha \ \varepsilon < V_D \rightarrow$ defacto 'evaporation criterion'

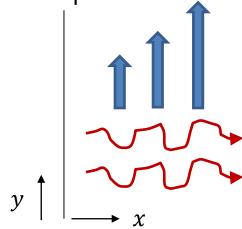
- → defines penetration depth of pulse
- Aim to characterize <u>statistics</u> of pulses, penetration depth distribution... in terms $Pdf(\tilde{\Gamma}_{0.e})$. Challenging...
 - → Meaningful output for SOL broadening problem

Spreading as Fluctuation Intensity Pulses, cont'd

- ~ 2D Model
- How address shearing → c.f. P.D., Hahm '95 → "Double" Burgers

$$\partial_t \tilde{\varepsilon} + V_D \partial_x \tilde{\varepsilon} + V_E(x) \partial_y \tilde{\varepsilon} + \alpha \, \tilde{\varepsilon} \partial_x \tilde{\varepsilon} - D_0 (\partial_x^2 + \partial_y^2) \tilde{\varepsilon} = 0$$

$$\tilde{\Gamma}(x = 0, y, t) \text{ specified}$$



• Shearing + scattering will couple $V_E(x)$ profile model required.

→ TBC...

Directed Percolation - Remark

- Recall Goldenfeld Rosenbluth lecture, Fest'17
 - Fundamentally, spreading as a directed percolation process...
- D.P. as P. with sense of time's arrow

c.f. PM Lecture as Intro to Percolation

- D.P. \leftrightarrow avalanching... \rightarrow pulses
- BTW '87 interprets SOC state as percolation cluster, critical to addition of single grain
- Mean field models of DP → reaction diffusion, hydrodynamics

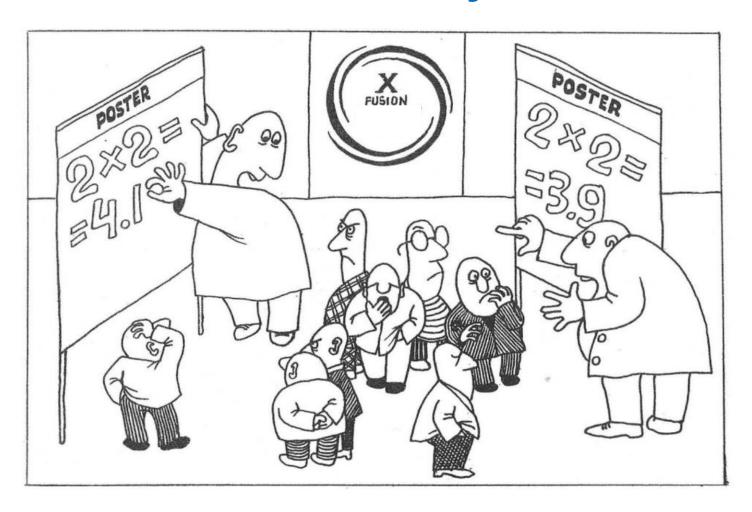
But...

- Fluctuations <u>significant</u> near criticality
 - → R. G. ... TBC ...

Philosophy

- MFE relevant questions within reach in near future. Great attention to λ_a problem (c.f. Samuel Johnson)
- Unreasonable for tokamak experiments to probe ~ critical dynamics so as to elucidate basic questions. Simulations???
- Well diagnosed, basic experiment with some relevant features are sorely needed – akin to 'Tube' studies of flows, ala' CSDX
- How?

Back to the Theory Festival!



Thank You!

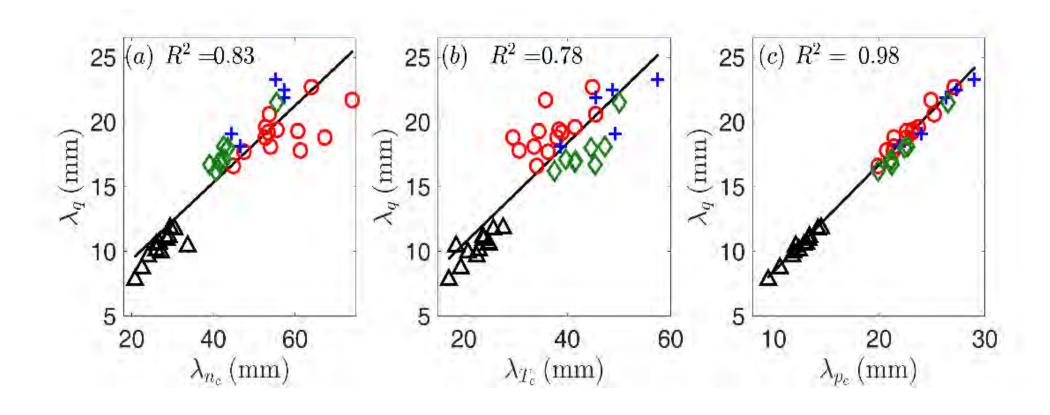
Supported by U.S. Dept. of

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Back-Up

$$\lambda_{n_e} \sim \lambda_{T_e} \sim \lambda_{P_e}$$



All SOL profiles scales comparable